

Name: _____

Exam Style Questions

Simultaneous Equations



Corbettmaths

Equipment needed: Calculator, pen

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents

Video 295



Answers and Video Solutions



1. Solve the simultaneous equations

$$\begin{array}{rcl} 5x + 3y & = & 41 \\ \text{sub} \quad 2x + 3y & = & 20 \\ \hline 3x & = & 21 \\ x & = & 7 \end{array}$$

$$\begin{array}{rcl} 5x + 3y & = & 41 \\ 35 + 3y & = & 41 \\ 3y & = & 6 \\ y & = & 2 \end{array}$$

check

$$2 \times 7 + 3 \times 2 \\ 14 + 6 = 20 \quad \checkmark$$

$$x = \underline{\quad 7 \quad} \quad y = \underline{\quad 2 \quad} \quad (3)$$

2. Solve the simultaneous equations

$$\begin{array}{rcl} 5x + y & = & 11 \\ \text{Add} \quad 3x - y & = & 9 \\ \hline 8x & = & 20 \\ x & = & 2.5 \end{array}$$

$$\begin{array}{rcl} 12.5 + y & = & 11 \\ y & = & -1.5 \end{array}$$

check

$$7.5 - (-1.5) = 9 \quad \checkmark$$

$$x = \underline{\quad 2.5 \quad} \quad y = \underline{\quad -1.5 \quad} \quad (3)$$

3. Solve the simultaneous equations

$$\begin{array}{r} x + 7y = 64 \\ \text{sub } x + 3y = 28 \\ \hline 4y = 36 \\ y = 9 \end{array}$$

$$\begin{array}{r} x + 63 = 64 \\ x = 1 \end{array}$$

Check

$$1 + 27 = 28 \quad \checkmark$$

$$x = \frac{1}{\dots\dots\dots} y = \frac{9}{\dots\dots\dots} \quad (3)$$

4. Solve the simultaneous equations

$$\begin{array}{r} 4x - 4y = 24 \\ \text{sub } x - 4y = 3 \\ \hline 3x = 21 \\ x = 7 \end{array}$$

$$\begin{array}{r} 28 - 4y = 24 \\ -4y = -4 \\ y = 1 \end{array}$$

$$7 - 4 = 3 \quad \checkmark$$

$$x = \frac{7}{\dots\dots\dots} y = \frac{1}{\dots\dots\dots} \quad (3)$$

5. Solve the simultaneous equations

$$\begin{array}{r} 2x + 4y = 14 \\ \text{Add } 4x - 4y = 4 \\ \hline 6x = 18 \\ x = 3 \end{array}$$

check $12 - 8 = 4 \checkmark$

$$\begin{array}{r} 6 + 4y = 14 \\ 4y = 8 \\ y = 2 \end{array}$$

$x = 3 \quad y = 2$
(3)

6. David buys 2 scones and 2 coffees in a shop and the cost is £18.
Ellie buys 3 scones and 2 coffees in the same shop and they cost £22.

Form two equations and solve to find the cost of each scone and each coffee.

$$\begin{array}{r} 3x + 2y = 22 \\ 2x + 2y = 18 \\ \hline x = 4 \end{array}$$

$$\begin{array}{r} 8 + 2y = 18 \\ 2y = 10 \\ y = 5 \end{array}$$

check $12 + 10 = 22 \checkmark$

Scone = £4 Coffee = £5
(4)

7. Alan and Connor have £6.70 in total.
Alan has £1.70 more than Connor.

Let a be the amount of money Alan has.
Let c be the amount of money Connor has.

Set up a pair of simultaneous equations and solve to find out how much each person has.

$$\begin{array}{r} a + c = 6.7 \\ \text{add } a - c = 1.7 \\ \hline 2a = 8.4 \\ a = 4.2 \end{array}$$

$$\begin{array}{r} 4.2 + c = 6.7 \\ c = 2.5 \end{array}$$

check ✓
 $4.2 - 2.5 = 1.7$

Alan = £4.20 Connor = £2.50

8. Solve the simultaneous equations

$$6x + y = -2$$

$$\begin{array}{r} \text{sub } 6x + y = -2 \\ 6x - 3y = 14 \\ \hline 4y = -16 \\ y = -4 \end{array}$$

$$6x - 4 = -2$$

$$6x = 2$$

$$x = \frac{1}{3}$$

check $2 + 12 = 14$ ✓

$x = \frac{1}{3}$ $y = -4$

(3)

9. Solve the simultaneous equations

$$2x + 4y = 26$$

$$3x - y = 4 \quad \times 4$$

$$12x - 4y = 16$$

$$\begin{array}{r} \text{Add} \quad 2x + 4y = 26 \\ \hline 14x = 42 \end{array}$$

$$x = 3$$

$$6 + 4y = 26$$

$$4y = 20$$

$$y = 5$$

check

$$9 - 5 = 4 \checkmark$$

$$x = \dots\dots\dots 3 \dots\dots\dots y = \dots\dots\dots 5 \dots\dots\dots$$

(3)

10. Solve the simultaneous equations

$$3x + 2y = 16 \quad \times 3$$

$$2x - 3y = 2 \quad \times 2$$

Do not use trial and improvement

$$9x + 6y = 48$$

$$\begin{array}{r} \text{Add} \quad 4x - 6y = 4 \\ \hline 13x = 52 \end{array}$$

$$x = 4$$

$$12 + 2y = 16$$

$$2y = 4$$

$$y = 2$$

check

$$8 - 6 = 2 \checkmark$$

$$x = \dots\dots\dots 4 \dots\dots\dots y = \dots\dots\dots 2 \dots\dots\dots$$

(4)

11. Solve the simultaneous equations

$$\begin{array}{r} 3x - 2y = 14 \\ \text{Add } x + 2y = 10 \\ \hline 4x = 24 \\ x = 6 \end{array}$$

check
 $18 - 4 = 14 \checkmark$

$$\begin{array}{r} 6 + 2y = 10 \\ 2y = 4 \\ y = 2 \end{array}$$

$$x = \dots\dots\dots 6 \dots\dots\dots y = \dots\dots\dots 2 \dots\dots\dots (3)$$

12. Solve the simultaneous equations

$$\begin{array}{r} 3x + 5y = 1 \quad \times 3 \\ 2x - 3y = 7 \quad \times 5 \\ \hline 9x + 15y = 3 \\ 10x - 15y = 35 \\ \hline 19x = 38 \\ x = 2 \end{array}$$

check
 $4 - (-3) = 7 \checkmark$

$$\begin{array}{r} 6 + 5y = 1 \\ 5y = -5 \\ y = -1 \end{array}$$

$$x = \dots\dots\dots 2 \dots\dots\dots y = \dots\dots\dots -1 \dots\dots\dots (4)$$

13. Solve the simultaneous equations

$$3x - y = 23 \quad \times 3$$

$$2x + 3y = 8$$

$$\begin{array}{r} 9x - 3y = 69 \\ 2x + 3y = 8 \\ \hline 11x = 77 \\ x = 7 \end{array}$$

$$\begin{array}{l} 14 + 3y = 8 \\ 3y = -6 \\ y = -2 \end{array}$$

check

$$21 - (-2) = 23 \quad \checkmark$$

$$x = \underline{7} \quad y = \underline{-2} \quad (3)$$

14. Solve the simultaneous equations

$$2y - 5x = 9 \quad \times 3$$

$$4y + 3x = 5 \quad \times 5$$

$$\begin{array}{r} 6y - 15x = 27 \\ 20y + 15x = 25 \\ \hline 26y = 52 \\ y = 2 \end{array}$$

$$\begin{array}{l} 8 + 3x = 5 \\ 3x = -3 \\ x = -1 \end{array}$$

~~4x - 5y = 9~~

$$4 - (-5) = 9 \quad \checkmark$$

$$x = \underline{-1} \quad y = \underline{2} \quad (3)$$

15. Solve the simultaneous equations

$$2x + 9y = 43 \quad \times 2$$

$$3x + 2y = 7 \quad \times 9$$

~~not the same~~

$$27x + 18y = 63$$

$$\begin{array}{r} \text{sub} \quad 4x + 18y = 86 \\ \hline 23x = -23 \end{array}$$

$$x = -1$$

$$-3 + 2y = 7$$

$$2y = 10$$

$$y = 5$$

check

$$-2 + 45 = 43 \quad \checkmark$$

$$x = \dots -1 \dots \quad y = \dots 5 \dots$$

(3)

16. Solve the simultaneous equations

$$5x - 3y = 24 \quad \times 4$$

$$2x - 4y = 4 \quad \times 3$$

$$20x - 12y = 96$$

$$\begin{array}{r} \text{sub} \quad 6x - 12y = 12 \\ \hline 14x = 84 \end{array}$$

$$x = 6$$

$$30 - 3y = 24$$

$$-3y = -6$$

$$y = 2$$

check

$$12 - 8 = 4 \quad \checkmark$$

$$x = \dots 6 \dots \quad y = \dots 2 \dots$$

(3)

17. A museum sells adult tickets or child tickets.

Fozia buys 4 ^x adult tickets and 1 ^y child ticket for £120

Sami buys 5 adult tickets and 3 child tickets for £171

Work out the cost of each type of ticket.

$$\begin{array}{rcl}
 4x + y & = & 120 \quad \times 3 \\
 5x + 3y & = & 171 \\
 \hline
 12x + 3y & = & 360 \\
 5x + 3y & = & 171 \\
 \hline
 7x & = & 189 \\
 x & = & 27
 \end{array}$$

$$\begin{array}{rcl}
 108 + y & = & 120 \\
 y & = & 12 \\
 \text{check} & & \\
 135 + 36 & = & 171
 \end{array}$$

Adult ticket £ ²⁷
 Child ticket £ ¹²
 (4)

18. Solve the simultaneous equations

$$\begin{array}{rcl}
 4x + 3y & = & 7.5 \quad \times 5 \\
 3x - 5y & = & 10.7 \quad \times 3
 \end{array}$$

$$\begin{array}{rcl}
 20x + 15y & = & 37.5 \\
 9x - 15y & = & 32.1 \\
 \hline
 29x & = & 69.6 \\
 x & = & 2.4
 \end{array}$$

$$\begin{array}{rcl}
 9.6 + 3y & = & 7.5 \\
 3y & = & -2.1 \\
 y & = & -0.7
 \end{array}$$

x = ^{2.4} y = ^{-0.7}
 (3)

19. Solve the simultaneous equations

$$2y = 8x + 11$$

$$2x + 8y = 27$$

$$8x - 2y = -11 \quad \times 4$$

$$32x - 8y = -44$$

$$\text{Add} \quad \begin{array}{r} 2x + 8y = 27 \\ \hline \end{array}$$

$$34x = -17$$

$$x = -0.5$$

$$-1 + 8y = 27$$

$$8y = 28$$

$$y = 3.5$$

$$2y - 11 = 8x$$

$$-11 = 8x - 2y$$

check

$$7 = -4 + 11 \quad \checkmark$$

$$x = -0.5 \quad y = 3.5$$

(3)

20. Find the coordinates of the point where the straight lines below cross.

$$y - 3x = 3$$

$$x - 2y = 4$$

$$-3x + y = 3 \quad \times 2$$

$$x - 2y = 4$$

$$\text{Add} \quad \begin{array}{r} -6x + 2y = 6 \\ \hline \end{array}$$

$$-5x = 10$$

$$x = -2$$

$$y + 6 = 3$$

$$y = -3$$

check

$$-2 + 6 = 4 \quad \checkmark$$

$$(-2, -3)$$

(4)

21. Solve the simultaneous equations

$$\begin{array}{r} 3a + c = 8 \\ \text{Add } 2a - c = 7 \\ \hline 5a = 15 \\ a = 3 \end{array}$$

$$\begin{array}{r} 9 + c = 8 \\ c = -1 \end{array}$$

$$6 - -1 = 7 \checkmark$$

$$a = \underline{\quad 3 \quad} \quad c = \underline{\quad -1 \quad}$$

(3)

22. Solve the simultaneous equations

$$\begin{array}{r} 9x - 6y = 114 \quad \times 3 \\ 5x - 9y = 30.75 \quad \times 2 \end{array}$$

$$\begin{array}{r} 27x - 18y = 342 \\ \text{sub } 10x - 18y = 61.5 \\ \hline 17x = 280.5 \\ x = 16.5 \end{array}$$

$$\begin{array}{r} 82.5 - 9y = 30.75 \\ -9y = -51.75 \\ y = 5.75 \end{array}$$

check

$$148.5 - 34.5 = 114 \checkmark$$

$$x = \underline{\quad 16.5 \quad} \quad y = \underline{\quad 5.75 \quad}$$

(4)

23. Solve the simultaneous equations

$$2y = x + 10$$

$$y = 2x - 7 \quad \times 2$$

$$\begin{array}{r} 2y = 4x - 14 \\ \text{sub } 2y = x + 10 \\ \hline 0 = 3x - 24 \end{array}$$

$$3x = 24$$

$$x = 8$$

$$2y = 8 + 10$$

$$2y = 18$$

$$y = 9$$

check

$$9 = 2 \times 8 - 7$$

$$9 = 16 - 7 \quad \checkmark$$

$$x = 8 \quad y = 9$$

(3)

24. Solve the simultaneous equations

$$4x - y = 17$$

$$y = x - 2$$

$$\begin{array}{r} -x + y = -2 \\ \text{Add } 4x - y = 17 \\ \hline 3x = 15 \\ x = 5 \end{array}$$

$$\text{sub into } 4x - y = 17$$

$$20 - y = 17$$

$$y = 3$$

check

$$3 = 5 - 2 \quad \checkmark$$

$$x = 5 \quad y = 3$$

(3)

25. x y
Three bananas and two pears cost £2.07
Five bananas and three pears cost £3.33

Find the cost of ten bananas and ten pears.

$$\begin{array}{rcl} 3x + 2y & = & 207 \quad \times 5 \\ 5x + 3y & = & 333 \quad \times 3 \end{array}$$

$$\begin{array}{rcl} 3x + 2y & = & 207 \\ 3x & = & 135 \\ x & = & 45 \end{array}$$

$$\begin{array}{rcl} 15x + 10y & = & 1035 \\ \text{sub } 15x + 9y & = & 999 \\ \hline y & = & 36 \end{array}$$

$$360 + 450 =$$

£8.10

(4)

26. Solve the simultaneous equations

$$\begin{array}{rcl} 5x + 2y & = & -34 \quad \times 3 \\ 4x - 3y & = & -41 \quad \times 2 \end{array}$$

check

$$-32 - 9 = -41$$

$$\begin{array}{rcl} 15x + 6y & = & -102 \\ \text{Add } 8x - 6y & = & -82 \\ \hline 23x & = & -184 \\ x & = & -8 \end{array}$$

$$\begin{array}{rcl} -40 + 2y & = & -34 \\ 2y & = & 6 \\ y & = & 3 \end{array}$$

$$x = \underline{-8} \quad y = \underline{3}$$

(4)

27. Albie is training for a marathon.
He jogs either route A or route B.

During April, he jogs route A nine times and route B five times.
Route B is 8 miles longer than route A.
In total, he jogs 89 miles in April.

In May, he will start jogging route C.
Route C is 20% longer than route B.

Work out the length of route C.

$$\begin{aligned} 9A + 5B &= 89 \\ B - A &= 8 \end{aligned}$$

$$\begin{aligned} 9A + 5B &= 89 \\ -A + B &= 8 \quad \times 9 \\ \hline -9A + 9B &= 72 \\ 9A + 5B &= 89 \\ \hline 14B &= 161 \\ B &= 11.5 \\ A &= 3.5 \end{aligned}$$

$$\begin{aligned} &13.8 \\ &\text{.....miles} \\ &(6) \end{aligned}$$

$$\begin{aligned} 10\% \text{ of } 11.5 &= 1.15 \\ 20\% \text{ of } 11.5 &= 2.3 \end{aligned}$$

$$11.5 + 2.3 = 13.8$$

28. Solve the simultaneous equations

$$6x + 2y = 13c$$

$$x + 2y = -2c$$

where c is a constant

Give your answers in terms of c .

$$\begin{array}{r} 6x + 2y = 13c \\ \text{Sub } x + 2y = -2c \\ \hline 5x = 15c \\ x = 3c \end{array}$$

$$3c + 2y = -2c$$

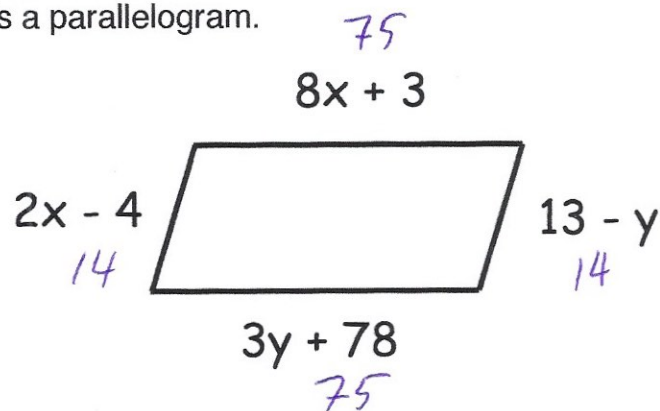
$$2y = -5c$$

$$y = -2.5c$$

$$\text{or} \\ y = -\frac{5}{2}c$$

$$x = 3c \quad y = -2.5c \quad (4)$$

29. Shown below is a parallelogram.



Work out the perimeter of the parallelogram.

$$8x + 3 = 3y + 78$$

$$8x - 3y = 75$$

$$2x - 4 = 13 - y$$

$$2x + y = 17$$

add

$$\begin{array}{r} 8x - 3y = 75 \\ 6x + 3y = 51 \\ \hline 14x = 126 \\ x = 9 \end{array}$$

$$18 + y = 17$$

$$y = -1$$

$$75 + 14 + 75 + 14$$

$$\dots\dots\dots 178 \text{ cm}$$

(6)